



**UNIVERSIDADE FEDERAL DE SANTA CATARINA  
CENTRO DE CIÊNCIAS FÍSICAS E MATEMÁTICAS  
PÓS-GRADUAÇÃO EM MATEMÁTICA PURA E APLICADA**

**MTM510012 Distribution Theory and Sobolev spaces**

Pre-requisite: MTM410029 Functional Analysis, Theory of measurement and integral of Lebesgue.

Weekly lesson hours: 06h

**Discipline syllabus:** The Function Space Tests. Density. Distributions in an open  $\Omega$  of  $\mathbb{R}^n$ . Derivation of distributions. Temperate Distributions. Fourier transform in  $L^1(\mathbb{R}^n)$ ,  $S(\mathbb{R}^n)$  and  $L^2(\mathbb{R}^n)$ . Fourier transform of tempered distributions. Plancherel's theorem. The Sobolev Spaces  $W(\Omega)$ . Properties, Reflexivity, Separability, Dual. The Space  $W(\Omega)$ . Prolonging Operators. The Sobolev spaces  $H^s(\Omega)$  and  $H^s(\Omega)$ ,  $s$  real,  $\Omega$  open subset of  $\mathbb{R}^n$ . The Trace Theorem. Applications to Partial Differential Equations. Generalized Solutions and Existence and Uniqueness of Initial and Border Value Problems.

**BIBLIOGRAPHIC REFERENCES**

1. Medeiros, L. A., Miranda, M. M., Espaços de Sobolev, 2a. Edição, Instituto de Matemática, UFRJ, 2004.
2. Brezis, H., Analyse Fonctionnelle: théorie et Applications, Masson (1983).
3. Kesavan, S., Topics in Functional Analysis and Applications, Wiley (1989).

**COMPLEMENTARY BIBLIOGRAPHY**

1. Adams, R. A., Sobolev Spaces, Academic Press (1975).
2. Evans, L. C., Partial differential equations, American Mathematical Society, 2002.
3. Hörmander, L., The Analysis of Linear Differential Operators I, Distribution Theory and Fourier Analysis, Springer-Verlag, 2ed., 1990
4. Medeiros, L. A. , Rivera, P. H. Iniciação aos Espaços de Sobolev, IM-UFRJ, Rio de Janeiro (1977).
5. Renardy, M., Rogers, R.C., An introduction to partial differential equations, Springer-Verlag, 1993.